

Method of the development of ontological operational semantics for imperative programming languages*

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Abstract. The paper presents a method of the development of operational semantics for imperative programming languages. It is based on the ontological approach to formal programming language specification implemented by information transition systems and conceptual transition systems. The method is illustrated by a fragment of the C language.

Keywords: operational semantics, ontological operational semantics, information transition system, conceptual transition system, C.

1. Introduction

Currently, there are tens of thousands of computer languages (programming languages, specification languages, domain-specific languages, scripting languages, markup languages, modeling languages, knowledge representation languages, and so on), and the creation of new computer languages continues. Formal methods are a means to ensure the correct and effective use of computer languages [2]. Application of formal methods to texts in these languages requires a formalization of these texts. Therefore, the development of formal semantics for computer languages is an important problem.

Operational semantics describing the abstract machine (AM[PL] for short) executing the instructions of a programming language (PL) on a set of states is generally used to formalize the language. The methodology for the development of the ontological operational semantics of PLs [1] based on conceptual transition systems (CTSs) was proposed in [3]. Like abstract state machines [4] (ASMs), CTSs allow states to be described in detail, but both these formalisms do not allow transitions to be described in detail. The languages AsmL [5] and XasM [6] based on ASMs are general-purpose languages for the specification of computer systems. They are not DSLs oriented to the description of transitions in AMs specifying operational semantics of PLs.

In this paper, we propose a method to elaborate this methodology. The development of operational semantics of a PL based on the method consists of two main stages. In the first stage, AM[PL] is described in the form of

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an information transition system [7] (ITS[PL]). ITSs are information models for a preliminary rough representation of the AMs structure. The purpose of the informal description is to classify the objects of AM[PL] as states, state objects, information queries, query objects, answers, and answer objects of ITS[PL]. The states, queries and answers of ITS[PL] describe the states, instructions and returning values of AM[PL], respectively. The state objects describe the objects observable in the states of AM[PL] (in particular, elements and substates of the states of AM[PL]). The query objects and answer objects of ITS[PL] describe the elements constituting the instructions and returning values of AM[PL], respectively. In the second stage, the formal conceptual information transition model [7] (CITM[PL]) of ITS[PL] in the language CTSL (Conceptual Transition System Language) [7] is defined. CITM[PL] includes representations of states, state objects, queries, query objects, answers, and answer objects in CTSL in the form of the conceptual structures (elements, conceptuials, concepts, attributes, individuals, conceptual states, and conceptual configurations) of CTSL, and an extension of CTSL [7] describing the operational semantics of query representations. Thus, the operational semantics of PL is defined in CTSL in conceptual (ontological) terms. Therefore, it is called the ontological operational semantics of PL [1].

The paper is organized as follows. Notions and denotations used in this paper are given in Section 2. The operational semantics method for programming languages based on CTSs is described in Section 3. Sections from 4 to 8 describe the stages of the development of operational semantics based on the method for a fragment of the C language (CF).

2. Preliminaries

Let O_b be the set of objects considered in this paper. Let S_t be a set of sets. Assume that I_{nt} , N_t , N_{t0} and B_l are the sets of integers, natural numbers, natural numbers with zero, and boolean values *true* and *false*, respectively. Let the names of sets be represented by capital letters, possibly with subscripts, and the elements of sets be represented by the corresponding small letters, possibly with extended subscripts. For example, i_{nt} and $i_{nt.1}$ are elements of I_{nt} .

Let $s_{t.(*)}$, $s_{t.\{*\}}$, and $s_{t.*}$ denote the sets of sequences of the forms $(o_{b.1}, \dots, o_{b.n_{t0}})$, $\{o_{b.1}, \dots, o_{b.n_{t0}}\}$, and $o_{b.1}, \dots, o_{b.n_{t0}}$ from elements of s_t .

The terms used in the paper are context-dependent. Contexts have the form $\llbracket o_{b.*} \rrbracket$, where the elements of $o_{b.*}$ called embedded contexts have the form $l_b:o_b$, l_b : or o_b . The elements of the set L_b are called labels. Let $o_b \llbracket o_{b.*} \rrbracket$ denote the object o_b in the context $\llbracket o_{b.*} \rrbracket$.

Let *und* denote the undefined value. Let F_n be a set of functions. Assume that $[f_n a_{rg.*}]$ is the application of f_n to $a_{rg.*}$. Let $[support f_n]$ denote the

support in $\llbracket f_n \rrbracket$, i.e., $[support\ f_n] = \{a_{rg} : [f_n\ a_{rg}] \neq und\}$.

Let A_{rg} and V_l be the sets of arguments and values. An object u_p of the form $a_{rg} : v_l$ is called an update. The objects a_{rg} and v_l are called the argument and the value in $\llbracket u_p \rrbracket$. Let U_p be a set of updates.

Let $[f_n\ u_p]$ denote the function $f_{n.1}$ such that $[f_{n.1}\ a_{rg}] = [f_n\ a_{rg}]$ if $a_{rg} \neq a_{rg}\llbracket u_p \rrbracket$ and $[f_{n.1}\ a_{rg}\llbracket u_p \rrbracket] = v_l\llbracket u_p \rrbracket$. Let $[f_n\ u_p, u_{p.*n_t}]$ be a shortcut for $\llbracket [f_n\ u_p]\ u_{p.*n_t} \rrbracket$; $[f_n\ a_{rg}.a_{rg.1} \dots .a_{rg.n_t} : v_l]$, for $[f_n\ a_{rg} : \llbracket [f_n\ a_{rg}]\ a_{rg.1} \dots .a_{rg.n_t} : v_l \rrbracket]$; and $[u_{p.*}]$ for $[f_n\ u_{p.*}]$, where $[support\ f_n] = \emptyset$.

Let S_{tt} , $O_{b.s}$, Q_r , $O_{b.q}$, A_{ns} and $O_{b.a}$ be the sets of states, state objects, queries, query objects, answers and answer objects. Let E_l , C_{nf} and S_{tr} be the sets of elements, conceptual configurations and conceptual structures (elements, conceptuls, concepts, attributes, individuals, conceptual states, conceptual configurations) of CTSL. Let L_n be a set of programming languages.

3. The method of the development of ontological operational semantics for imperative programming languages

The development of operational semantics of l_n in CTSL includes the following stages:

1. Describe $AM[l_n]$ in the form of an $ITS[l_n]$.
 - (a) Describe the sets of proper state objects. An object $o_{b.s}$ is a proper state object if $o_{b.s} \notin S_{tt}$.
 - (b) Describe the sets of states.
 - (c) Describe the sets of proper answer objects. An object $o_{b.a}$ is a proper answer object if $o_{b.a} \notin A_{ns}$.
 - (d) Describe the sets of answers.
 - (e) Describe the sets of proper query objects. An object $o_{b.q}$ is a proper query object if $o_{b.q} \notin Q_r$.
 - (f) Describe the sets of queries.
2. Define $CITM[l_n]$ of $ITS[l_n]$. The CTS of $CITM[l_n]$ denoted by $CTSL[l_n]$ is an extension of CTSL. The extension defines the operational semantics of l_n in CTSL, and the model describes the correspondence between the objects of $AM[l_n]$ and conceptual structures of CTSL.
 - (a) Define the set of conceptual structures of CTSL representing proper state objects of $ITS[l_n]$ in $CTSL[l_n]$.
 - (b) Define the set of conceptual configurations representing the states of $ITS[l_n]$ in $CTSL[l_n]$. The set of conceptual structures representing the state objects of $ITS[l_n]$ is called an ontology of l_n in CTSL.

Therefore, the operational semantics of l_n in CTSL is called an ontological operational semantics of l_n .

- (c) Define the set of elements representing the proper answer objects of $\text{ITS}[l_n]$ in $\text{CTSL}[l_n]$.
- (d) Define the set of elements representing the answers of $\text{ITS}[l_n]$ in $\text{CTSL}[l_n]$.
- (e) Define the set of elements in $s_{s.t.c}$ representing the proper query objects of $\text{ITS}[l_n]$ in $\text{CTSL}[l_n]$.
- (f) Define the set of defined elements in $\text{CTSL}[l_n]$ representing the queries of $\text{ITS}[l_n]$ in $\text{CTSL}[l_n]$.
- (g) Define the element interpretation order [8], exogenous transition order [7] and endogenous transition order [7] in $\text{CTSL}[l_n]$. They describe the order of execution of element interpretations and transitions.

Let $r_{p.s} \in O_{b.s} \rightarrow S_{tr}$, $r_{p.q} \in O_{b.q} \rightarrow E_l$ and $r_{p.a} \in O_{b.a} \rightarrow E_l$ be the representation functions of state objects, query objects and answer objects of $\text{ITS}[l_n]$ in CTSL . Let $r_{p.s}^-$, $r_{p.q}^-$ and $r_{p.a}^-$ be inverse functions of $r_{p.s}$, $r_{p.q}$ and $r_{p.a}$.

In the following sections, we apply the method to the development of ontological operational semantics for a fragment of the C language defined by an abstract machine $\text{AM}[C]$.

4. Description of $\text{ITS}[C]$

The set of proper state objects of $\text{ITS}[C]$ includes the objects of $\text{AM}[C]$ such as names, types, addresses and their values, variables and their attributes (names, values, types, addresses), functions and their attributes (names, parameters, parameter types, return values, bodies), call levels, relative variable scopes.

A call level specifies the number of nested function calls. A relative variable scope specifies the number of block nesting. The scope 0 is associated with global variables, and the other scopes are associated with local variables.

The state of $\text{ITS}[C]$ specifies the current variable scope, the current call level and relations between the following objects: addresses and their values, variables and their attributes, functions and their attributes.

The set of answers of $\text{ITS}[C]$ includes the values of C types, the jumps initiated by jump statements and the program error message.

The set of queries of $\text{ITS}[C]$ includes the instructions of $\text{AM}[C]$ such as statements, expressions (built of variables, literals, and operators), declarations, conversions, and programs.

AM[C] contains extra instructions in addition to C instructions. The extra instructions includes C expressions extended by new literals such as pointer literals, array literals, structure literals, union literals and function literals representing the values of pointer types, array types, structure types, union types, and function types, respectively, and also the dynamic memory management instructions *new* and *delete* from the C-light language [9].

5. Proper state objects in CTSL[C]

A name is represented by an instance of the concept *name* defined by the rule

(rule (*x is name*) var (*x*) abn then (*x is normal*)).

The syntax and semantics of rules are defined in [7]. The predefined CTSL element (*e_l is normal*) specifies that *e_l* is a normal element [8]. Thus, names are represented by normal elements. Let $N_m = [content\ name]$. The object $[content\ c_{ncp}]$ denotes the content (the set of instances) of the concept c_{ncp} .

A label is represented by an instance of the concept *label* defined by the rule

(rule (*x is label*) var (*x*) abn then
(*x matches y :: label* var (*y*) where (*y is name*))).

The predefined CTSL element (*e_l matches p_{tt} var (v_{r,*}) where c_{nd}*) specifies that the element *e_l* matches the pattern *p_{tt}* with the variables *v_{r,*}* and the condition *c_{nd}* is true for the corresponding values of these variables. Let $L_b = [content\ label]$.

A type is represented by an instance of the concept *type-literal* defined by the rule

(rule (*x is type-literal*) var (*x*) abn then
(*x is basic-type*) or (*x is derived-type-literal*))).

The predefined CTSL element (*c_{nd.1} or c_{nd.2}*) specifies the disjunction of the conditions *c_{nd.1}* and *c_{nd.2}*. The false and true values are defined in CTSL as follows: the element *und* is the false value, and any element distinct from *und* is the true value.

A basic type is represented by an instance of the concept *basic-type* defined by the rule

(rule (*x is basic-type*) var (*x*) abn then
(*x :: q in :: set (int, float, ...) :: q*)),

where *int, float, ...* is a sequence of all basic types of C. The predefined CTSL element (*e_l in :: set (e_{l,*})*) specifies that *e_l* is an element of the sequence *e_{l,*}*. The element of the form *e_l :: q* is called a quoted element.

The value of the quoted element $e_l :: q$ in CTSL is defined as e_l . Let $T_{p.b} = [\text{content basic-type}]$.

A derived type is represented by an instance of the concept *derived-type-literal* defined by the rule

(rule (*x is derived-type-literal*) var (*x*) abn then
 (*x is pointer-type-literal*) or (*x is array-type-literal*) or
 (*x is structure-type-literal*) or (*x is function-type-literal*)).

An array type is represented by an instance of the concept *array-type-literal* defined by the rule

(rule (*x is array-type-literal*) var (*x*) abn then
 (*x matches (array y) where (y is type-literal)*)).

A structure type is represented by an instance of the concept *structure-type-literal* defined by the rule

(rule (*x is structure-type-literal*) var (*x*) abn
 then (*x matches y :: structure-type var (y)*)).

Let $T_{p.s} = [\text{content structure-type-literal}]$.

A pointer type is represented by an instance of the concept *pointer-type-literal* defined by the rule

(rule (*x is pointer-type-literal*) var (*x*) abn then
 (*x matches (pointer y) where (y is type-literal)*)).

A function type is represented by an instance of the concept *function-type-literal* defined by the rule

(rule (*x is function-type*) var (*x*) abn then
 (*x matches (function y z) var (y, z)*
 where ((*y is (sequence type-literal)*) and (*z is type-literal*)))).

The predefined CTSL element ($c_{nd.1}$ and $c_{nd.2}$) specifies the conjunction of the conditions $c_{nd.1}$ and $c_{nd.2}$.

A type in $[[s_{tt}[\text{ITS}[C]]]]$ is represented by an instance of the concept *type* in $[[[r_{p.s} s_{tt}]]]$ defined by the rule

(rule (*x is type*) var (*x*) abn then
 (*x is basic-type*) or (*x is derived-type*)).

A derived type in $[[s_{tt}[\text{ITS}[C]]]]$ is represented by an instance of the concept *derived-type* in $[[[r_{p.s} s_{tt}]]]$ defined by the rule

(rule (*x is derived-type*) var (*x*) abn then
 (*x is pointer-type*) or (*x is array-type*) or
 (*x is structure-type*) or (*x is function-type*)).

An array type in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept *array-type* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is array-type*) var (*x*) abn then
(*x matches (array y) where (y is type)*)).

The conceptual $(0 : t_{p.s}, 1 : \text{structure-type})$ in $\llbracket c_{nf} \rrbracket$ represents the structure type $t_{p.s}$ in $\llbracket [r_{p.s} c_{nf}] \rrbracket$. A structure type $t_{p.s}$ is a structure type in c_{nf} if $[c_{nf} (0 : t_{p.s}, 1 : \text{structure-type})] \neq \text{und}$. The conceptual $(-1 : \text{body}, 0 : t_{p.s}, 1 : \text{structure-type})$ in c_{nf} represents a body, fields and their types in $\llbracket [t_{p.s}, r_{p.s} c_{nf}] \rrbracket$. An element b_d is a body in $\llbracket [t_{p.s}, c_{nf}] \rrbracket$ if $[c_{nf} (-1 : \text{body}, 0 : t_{p.s}, 1 : \text{structure-type})] = b_d$. The element b_d is an attribute element. The attribute element with the attributes $a_{tt.1}, \dots, a_{tt.n_{t0}}$ has the form $(a_{tt.1} : v_{l.1}, \dots, a_{tt.n_{t0}} : v_{l.n_{t0}})$, where $v_{l.1}, \dots, v_{l.n_{t0}}$ are the values of the attributes $a_{tt.1}, \dots, a_{tt.n_{t0}}$. The attribute element can be considered as a function mapping the attributes to their values. A field f_l is a field in $\llbracket [t_{p.s}, c_{nf}] \rrbracket$ if $[c_{nf} (-1 : \text{body}, 0 : t_{p.s}, 1 : \text{structure-type})] f_l] \neq \text{und}$. A type t_p is a type in $\llbracket [f_l, t_{p.s}, c_{nf}] \rrbracket$ if $[c_{nf} (-1 : \text{body}, 0 : t_{p.s}, 1 : \text{structure-type})] f_l] = t_p$.

A structure type in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept *structure-type* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is structure-type*) var (*x*) abn
then ((*x is structure-literal*) and $(0 : x, 1 : \text{structure-type})$)).

A field in $\llbracket [r_{p.s}^- t_{p.s}] \rrbracket$ in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept (*field in $t_{p.s}$*) in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is (field in y)*) var (*x, y*) abn then
((*x is field-literal*) and
($(-1 : \text{body}, 0 : y, 1 : \text{structure-type}) .. x$))).

The predefined CTSL element $(e_{l.a} .. a_{tt})$ specifies the value of the attribute a_{tt} of the attribute element $e_{l.a}$.

A pointer type in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept *pointer-type* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is pointer-type*) var (*x*) abn then
(*x matches (pointer y) where (y is type)*)).

A function type in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept *function-type* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is function-type*) var (*x*) abn then
(*x matches (function y z) var (y, z)*
where ((*y is (sequence type)*) and (*z is type*))).

The predefined CTSL element (e_l is (sequence c_{ncp})) specifies that e_l is a sequence of the instances of the concept c_{ncp} .

A variable is represented by an instance of the concept *variable-literal* defined by the rule

(rule (x is *variable-literal*) abn var (x) then
(x matches $y :: variable$ var (y) where (y is name))).

Let $V_r = [content\ variable-literal]$.

A relative variable scope is represented by an instance of the concept *scope* defined by the rule

(rule (x is *scope*) var (x) abn then (x is $nat0$)).

The predefined CTSL element (e_l is $nat0$) specifies that $e_l \in N_{t0}$. Let $S_{cp} = [content\ scope]$.

An array is represented by an instance of the concept *array-literal* defined by the rule

(rule (x is *array-literal*) var (x) abn
then (x matches $y :: array$ var (y) where (y is nat))).

The predefined CTSL element (e_l is nat) specifies that $e_l \in N_t$. Let $A_{rr} = [content\ array-literal]$.

A structure is represented by an instance of the concept *structure-literal* defined by the rule

(rule (x is *structure-literal*) var (x) abn
then (x matches $y :: structure$ var (y) where (y is nat))).

Let $S_{trc} = [content\ structure-literal]$.

A field is represented by an instance of the concept *field-literal* defined by the rule

(rule (x is *field-literal*) var (x) abn then
(x matches $y :: field$ var (y))).

Let $F_l = [content\ field-literal]$.

A function is represented by an instance of the concept *function-literal* defined by the rule

(rule (x is *function-literal*) var (x) abn then
(x matches $y :: function$ var (y) where (y is name))).

Let $F_n = [content\ function-literal]$.

A formal argument of a function is represented by an instance of the concept *argument* defined by the rule

(rule (*x is argument*) var (*x*) abn then
(*x is variable-literal*)).

Thus, formal function arguments are represented by variables. Let $A_{rg} =$ [*content argument*].

A call level is represented by an instance of the concept *call-level* defined by the rule

(rule (*x is call-level*) var (*x*) abn then (*x is nat0*)).

Let $L_{v.c} =$ [*content call-level*].

A pointer is represented by an instance of the concept *pointer-literal* defined by the rule

(rule (*x is pointer-literal*) var (*x*) abn then
((*x is typed-pointer-literal*) or (*x is variable-pointer-literal*) or
(*x is function-pointer-literal*) or (*x is array-pointer-literal*) or
(*x is structure-pointer-literal*) or (*x :: q = null*))).

Let $P_n =$ [*content pointer-literal*]. These pointers are smart, i.e., they 'know' their types and their connections with variables, arrays, structures, unions, and functions.

The concept *typed-pointer-literal* is defined by the rule

(rule (*x is typed-pointer-literal*) var (*x*) abn
then (*x matches (id : y, type : z) :: pointer var (y)*
where ((*y is nat0*) and (*z is type*)))).

Let $P_{n.t} =$ [*content typed-pointer-literal*].

The concept *variable-pointer-literal* is defined by the rule

(rule (*x is variable-pointer-literal*) var (*x*) abn then
(*x matches (variable : y, scope : z, call-level : u) :: pointer*
var (*y, z, u*) where ((*y is variable-literal*) and (*z is scope*) and
(*u is call-level*)))).

Let $P_{n.v} =$ [*content variable-pointer-literal*].

The concept *array-pointer-literal* is defined by the rule

(rule (*x is array-pointer-literal*) var (*x*) abn then
(*x matches (array : y, index : z) :: pointer var (y, z)*
where ((*y is array-literal*) and (*z is nat0*)))).

Let $P_{n.a} =$ [*content array-pointer-literal*].

The concept *structure-pointer-literal* is defined by the rule

(rule (*x is structure-pointer-literal*) var (*x*) abn then
(*x matches (structure : y, field : z) :: pointer var (y, z)*
where ((*y is structure-literal*) and (*z is field-literal*)))).

Let $P_{n.s} = [\text{content structure-pointer-literal}]$.

The concept *function-pointer-literal* is defined by the rule

(rule (*x is function-pointer-literal*) var (*x*) abn then
 (*x matches (function : y, types : z) :: pointer var (y, z)*
 where ((*y is function-literal*) and (*z is (sequence type)*))))).

Let $P_{n.f} = [\text{content function-pointer-literal}]$.

The conceptual $(0 : p_{n.t}, 1 : \text{pointer})$ in $\llbracket c_{nf} \rrbracket$ represents the pointer $p_{n.t}$ in $\llbracket [r_{p.s}^- c_{nf}] \rrbracket$. A pointer $p_{n.t}$ is a pointer in $\llbracket c_{nf} \rrbracket$ if $[c_{nf} (0 : p_{n.t}, 1 : \text{pointer})] \neq \text{und}$. The conceptual $(-1 : \text{value}, 0 : p_{n.t}, 1 : \text{pointer})$ in $\llbracket c_{nf} \rrbracket$ represents a value in $\llbracket [p_{n.t}, [r_{p.s}^- c_{nf}]] \rrbracket$. An element v_l is a value in $\llbracket [p_{n.t}, c_{nf}] \rrbracket$ if $v_l = [c_{nf} (-1 : \text{value}, 0 : p_{n.t}, 1 : \text{pointer})]$.

A pointer in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept *pointer* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is pointer*) var (*x*) abn then
 ((*x is pointer-literal*) and
 ((*x is typed-pointer*) \Rightarrow ($0 : x, 1 : \text{pointer}$))))).

The predefined CTSL element ($c_{nd.1} \Rightarrow c_{nd.2}$) specifies that $c_{nd.1}$ implies $c_{nd.2}$.

The conceptual $(0 : a_{rr}, 1 : \text{array})$ in $\llbracket c_{nf} \rrbracket$ represents the array a_{rr} in $\llbracket [r_{p.s}^- c_{nf}] \rrbracket$. An array a_{rr} is an array in $\llbracket c_{nf} \rrbracket$ if $[c_{nf} (0 : a_{rr}, 1 : \text{array})] \neq \text{und}$. The conceptual $(-1 : \text{element-type}, 0 : a_{rr}, 1 : \text{array})$ in $\llbracket c_{nf} \rrbracket$ represents an element type and a type in $\llbracket [a_{rr}, [r_{p.s}^- c_{nf}]] \rrbracket$. A type t_p is an element type in $\llbracket [a_{rr}, c_{nf}] \rrbracket$ if $[c_{nf} (-1 : \text{element-type}, 0 : a_{rr}, 1 : \text{array})] = t_p$. A type $(\text{array } t_p)$ is a type in $\llbracket [a_{rr}, c_{nf}] \rrbracket$ if t_p is an element type in $\llbracket [a_{rr}, c_{nf}] \rrbracket$. The conceptual $(-1 : \text{body}, 0 : a_{rr}, 1 : \text{array})$ in $\llbracket c_{nf} \rrbracket$ represents elements in $\llbracket [a_{rr}, [r_{p.s}^- c_{nf}]] \rrbracket$. A sequence element b_d is a body in $\llbracket [a_{rr}, c_{nf}] \rrbracket$ if $b_d = [c_{nf} (-1 : \text{body}, 0 : a_{rr}, 1 : \text{array})]$. The element e_l is an element in $\llbracket [a_{rr}, c_{nf}, n_t] \rrbracket$ if $\llbracket [c_{nf} (-1 : \text{body}, 0 : a_{rr}, 1 : \text{array})] \cdot [n_{t0} + 1] \rrbracket = e_l$, and $0 \leq n_{t0} < \llbracket \text{len } [c_{nf} (-1 : \text{body}, 0 : a_{rr}, 1 : \text{array})] \rrbracket$. The element e_l is an element in $\llbracket [a_{rr}, c_{nf}] \rrbracket$ if e_l is an element in $\llbracket [a_{rr}, c_{nf}, n_{t0}] \rrbracket$ for some n_{t0} .

An array in $\llbracket s_{tt}[\text{ITS}[C]] \rrbracket$ is represented by an instance of the concept *array* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is array*) var (*x*) abn
 then ((*x is array-literal*) and ($0 : x, 1 : \text{array}$))).

The conceptual $(0 : s_{trc}, 1 : \text{structure})$ in $\llbracket c_{nf} \rrbracket$ represents the structure in $\llbracket [r_{p.s}^- c_{nf}] \rrbracket$. A structure s_{trc} is a structure in $\llbracket c_{nf} \rrbracket$ if $[c_{nf} (0 : s_{trc}, 1 : \text{structure})] \neq \text{und}$. The conceptual $(-1 : \text{type}, 0 : s_{trc}, 1 : \text{structure})$ in $\llbracket c_{nf} \rrbracket$ represents a type in $\llbracket [s_{trc}, [r_{p.s}^- c_{nf}]] \rrbracket$. A type $t_{p.s}$ is a type in $\llbracket [s_{trc}, c_{nf}] \rrbracket$ if $[c_{nf} (-1 : \text{type}, 0 : s_{trc}, 1 : \text{structure})] = t_{p.s}$. The conceptual $(-1 : \text{body}, 0 : s_{trc}, 1 : \text{structure})$ in $\llbracket c_{nf} \rrbracket$ represents a body, fields

and their values in $\llbracket s_{trc}, [r_{p.s}^- c_{nf}] \rrbracket$. An element b_d is a body in $\llbracket s_{trc}, c_{nf} \rrbracket$ if $[c_{nf} (-1 : body, 0 : s_{trc}, 1 : structure)] = b_d$. A field f_l is a field in $\llbracket s_{trc}, c_{nf} \rrbracket$ if $\llbracket [c_{nf} (-1 : body, 0 : s_{trc}, 1 : structure)] f_l \rrbracket \neq und$. An element v_l is a value in $\llbracket f_l, t_{p.s}, c_{nf} \rrbracket$ if $\llbracket [c_{nf} (-1 : body, 0 : s_{trc}, 1 : structure)] f_l \rrbracket = v_l$.

A structure in $\llbracket s_{tt} \llbracket ITS[C] \rrbracket \rrbracket$ is represented by an instance of the concept *structure* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is structure*) var (*x*) abn
then ((*x is structure-literal*) and ($0 : x, 1 : structure$))).

The information about functions is represented by the substate *function* in configurations. The conceptual $(-1 : t_{p.(*)}, 0 : f_n, 1 : function) :: state :: function$ in $\llbracket c_{nf} \rrbracket$ represents the function $[r_{p.s}^- f_n]$ with the argument types $[r_{p.s}^- t_{p.(*)}]$ in $\llbracket [r_{p.s}^- c_{nf}] \rrbracket$. A function f_n is a function in $\llbracket t_{p.(*)}, c_{nf} \rrbracket$ if $[c_{nf} (-1 : t_{p.(*)}, 0 : f_n, 1 : function) :: state :: function] \neq und$. An element $t_{p.(*)}$ is an argument type sequence in $\llbracket f_n, c_{nf} \rrbracket$ if f_n is a function in $\llbracket t_{p.(*)}, c_{nf} \rrbracket$. The conceptual $(-2 : arguments, -1 : t_{p.(*)}, 0 : f_n, 1 : function) :: state :: function$ in $\llbracket c_{nf} \rrbracket$ represents arguments in $\llbracket [r_{p.s}^- f_n], [r_{p.s}^- c_{nf}] \rrbracket$. An element $a_{rg.(*)}$ is an argument sequence in $\llbracket f_n, c_{nf} \rrbracket$ if $[c_{nf} (-2 : arguments, -1 : t_{p.(*)}, 0 : f_n, 1 : function) :: state :: function] = a_{rg.(*)}$. The conceptual $(-2 : return-type, -1 : t_{p.(*)}, 0 : f_n, 1 : function) :: state :: function$ in $\llbracket c_{nf} \rrbracket$ represents the return type in $\llbracket [r_{p.s}^- f_n], [r_{p.s}^- c_{nf}] \rrbracket$. A type t_p is the return type in $\llbracket f_n, c_{nf} \rrbracket$ if $[c_{nf} (-2 : return-type, -1 : t_{p.(*)}, 0 : f_n, 1 : function) :: state :: function] = t_p$. The conceptual $(-2 : body, -1 : t_{y.(*)}, 0 : f_n, 1 : function) :: state :: function$ in $\llbracket c_{nf} \rrbracket$ represents a body in $\llbracket [r_{p.s}^- f_n], [r_{p.s}^- c_{nf}] \rrbracket$. An element b_d is a body in $\llbracket f_n, c_{nf} \rrbracket$ if $[c_{nf} (-2 : body, -1 : t_{y.(*)}, 0 : f_n, 1 : function) :: state :: function] = b_d$.

The conceptals $(0 : level) :: state :: function$ and $(0 : type) :: state :: function$ specify the current call level and the return type in it, respectively.

The conceptual $(-2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)$ in $\llbracket c_{nf} \rrbracket$ represents the variable $[r_{p.s}^- v_r]$ in $\llbracket [l_{v.c}, s_{cp}, [r_{p.s}^- c_{nf}]] \rrbracket$. A variable v_r is a variable in $\llbracket [l_{v.c}, s_{cp}, c_{nf}] \rrbracket$ if $[c_{nf} (-2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)] \neq und$. The conceptual $(-3 : pointer, -2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)$ in $\llbracket c_{nf} \rrbracket$ represents an address in $\llbracket [r_{p.s}^- v_r], l_{v.c}, s_{cp}, [r_{p.s}^- c_{nf}] \rrbracket$. A pointer $p_{n.v}$ is a pointer in $\llbracket v_r, l_{v.c}, s_{cp}, c_{nf} \rrbracket$ if $[c_{nf} (-3 : pointer, -2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)] = p_{n.v}$. The conceptual $(-3 : type, -2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)$ in $\llbracket c_{nf} \rrbracket$ represents a type in $\llbracket [r_{p.s}^- v_r], l_{v.c}, s_{cp}, [r_{p.s}^- c_{nf}] \rrbracket$. A type t_p is a type in $\llbracket v_r, l_{v.c}, s_{cp}, c_{nf} \rrbracket$ if $[c_{nf} (-3 : type, -2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)] = t_p$. The conceptual $(-3 : value, -2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)$ in $\llbracket c_{nf} \rrbracket$ represents a value in $\llbracket [r_{p.s}^- v_r], l_{v.c}, s_{cp}, [r_{p.s}^- c_{nf}] \rrbracket$. An element v_l is a value in $\llbracket v_r, l_{v.c}, s_{cp}, c_{nf} \rrbracket$ if $[c_{nf} (-3 : value, -2 : l_{v.c}, -1 : s_{cp}, 0 : v_r, 1 : variable)] = v_l$.

The information about blocks is represented by the substate *block* in configurations. The conceptual $(0 : scope) :: block$ specifies the current

relative scope.

A name n_m can have a set of possible values in $\llbracket c_{nf} \rrbracket$. For example, possible values of the name v_r of the form $n_{m.1} :: \text{variable}$ in $\llbracket c_{nf} \rrbracket$ are the variables with the name $n_{m.1}$ of scopes from 0 to the current scope in $\llbracket c_{nf} \rrbracket$. To choose the right value in $\llbracket name : n_m, c_{nf} \rrbracket$ and, thus, to resolve the name conflict, these possible values are indexed. For example, indices in $\llbracket name : v_r, c_{nf} \rrbracket$ are scopes from 0 to the current scope in $\llbracket c_{nf} \rrbracket$. Then the name resolution problem is reduced to the choice of a right index in $\llbracket name : n_m, c_{nf} \rrbracket$.

A variable in $\llbracket s_{tt} \llbracket ITS[C] \rrbracket \rrbracket$ is represented by an instance of the concept *variable* in $\llbracket [r_{p.s} s_{tt}] \rrbracket$ defined by the rule

(rule (*x is variable*) var (*x*) abn then (*index in x*)).

The element (*index in v_r*) returning the right index in $\llbracket v_r, c_{nf} \rrbracket$ is defined by the rules

(rule (*index in x*) var (*x*) abn where (*x is variable-literal*)
then (let :: seq (*w1*, *w2*) be (*current-scope*, *current-call-level*) in
(*index in x in w1*, *w2*)));
(rule (*x is index in y, z*) var (*x, y, z*) abn then
(if ($-2 : y$, $-1 : z$, $0 : x$, $1 : \text{variable}$) then $z :: q$ else
(if ($z = 0$) then und else
(let *w* be ($z - 1$) in (*index in x in y, w*))))).

The predefined CTSL element (*let :: seq ($v_{r.*}$) be ($e_{l.*}$) in b_d*), where $b_d \in E_{l.*}$, replaces the variables $v_{r.*}$ in the body b_d by the values of the corresponding elements of $e_{l.*}$ and executes the resulting body.

The elements *current-scope* and *current-call-level* are defined by the rules

(rule *current-scope* then ($0 : \text{scope}$) :: *state* :: *block*);
(rule *current-scope* then ($0 : \text{call-level}$) :: *state* :: *function*).

A variable v_r is global in $\llbracket c_{nf} \rrbracket$ if the right index in $\llbracket v_r, c_{nf} \rrbracket$ equals 0. A variable v_r is local in $\llbracket c_{nf} \rrbracket$ if the right index in $\llbracket v_r, c_{nf} \rrbracket$ is greater than 0. The type and value of a global variable v_r in $\llbracket c_{nf} \rrbracket$ is specified by the conceptals ($-3 : \text{type}$, $-2 : 0$, $-1 : 0$, $0 : v_r$, $1 : \text{variable}$) and ($-3 : \text{value}$, $-2 : 0$, $-1 : 0$, $0 : v_r$, $1 : \text{variable}$), respectively.

A value is represented by an instance of the concept *value-literal* defined by the rule

(rule (*x is value-literal*) var (*x*) abn then
((*x is int*) or (*x is float*) or ... or
(*x is pointer-literal*) or (*x is array-literal*) or
(*x is structure-literal*) or (*x is function-literal*))),

where ... are disjuncts of the form $(x \text{ is } t_{p,b})$ for all $t_{p,b}$. Let $V_l = [\text{content value-literal}]$.

A value in $\llbracket s_{tt} \llbracket \text{ITS}[C] \rrbracket \rrbracket$ is represented by an instance of the concept *value* in $\llbracket [r_{p,s} s_{tt}] \rrbracket$ defined by the rule

(rule $(x \text{ is value}) \text{ var } (x) \text{ abn then}$
 $((x \text{ is int}) \text{ or } (x \text{ is float}) \text{ or } \dots \text{ or}$
 $(x \text{ is pointer}) \text{ or } (x \text{ is array}) \text{ or}$
 $(x \text{ is structure}) \text{ or } (x \text{ is function})))$,

where ... are disjuncts of the form $(x \text{ is } t_{p,b})$ for all $t_{p,b}$.

6. States in CTSL[C]

States are represented by configurations including the substates *block* and *function* and conceptals defined in Section 5. These substates model information associated with blocks and functions, respectively.

7. Answers in CTSL[C]

The element of the form $e_l :: ex$ is called an exception. The value of the exception $e_l :: ex$ in CTSL is defined as $e_l :: ex$. The exceptions $(\text{type} : \text{break}) :: ex$, $(\text{type} : \text{continue}) :: ex$ and $(\text{type} : \text{goto}, \text{label} : l_b) :: ex$ represent the execution of the *break* statement, the *continue* statement, and the *goto* statement with the label l_b , respectively. The exceptions $(\text{type} : \text{return}, \text{value} : v_l) :: ex$ and $(\text{type} : \text{return}) :: ex$ represent the execution of the *return* statement. These exceptions are called jumps.

The values of C types are represented by instances of the concept *value-literal*, the extra literals of AM[C] are represented by instances of the corresponding concepts, jumps initiated by jump statements are represented by jump exceptions, and the program error message is represented by *und*.

8. Defined elements in CTSL[C]

8.1. Statements and blocks

The elements *break*, *continue* and $(\text{goto } l_b)$ representing the queries *break*;; *continue*; and *goto* $[r_{p,q} l_b]$; are defined by the rules

(rule *break* abn then $(\text{type} : \text{break}) :: ex$);
(rule *continue* abn then $(\text{type} : \text{continue}) :: ex$);
(rule $(\text{goto } x) \text{ var } (x) \text{ abn where } (x \text{ is label}) \text{ then}$
 $(\text{type} : \text{goto}, \text{label} : x) :: ex$).

The element $n_m :: \text{label}$ representing queries of the form $[r_{p,q} n_m : s_{ttm};]$ as $(\text{seq } n_m :: \text{label } [r_{p,q} s_{ttm}])$ is defined by the rule

(rule $x :: \text{label } \text{var } (x) \text{ und then } (\text{catch } w$
 (if $w \text{ matches } (\text{type} : \text{goto}, \text{label} : y :: \text{label}) \text{ var } (y)$
 where $(y :: q = x :: q) \text{ then else } (\text{throw } w :: q))))$).

The predefined CTSL element ($\text{throw } e_l$) assigns the value of the element e_l to a special conceptual $(0 : ()) :: \text{state} :: \text{value}$ specifying the current value of the CTS CTSL[C]. The predefined CTSL element ($\text{catch } v_r \ e_{l.*}$) replaces the variable v_r in the sequence e_l by the value of the conceptual $(0 : ()) :: \text{state} :: \text{value}$ and executes the resulting sequence. The predefined CTSL element ($\text{if } e_l \text{ matches } p_{tt} \text{ var } (v_{r.*}) \text{ where } c_{nd} \text{ then } e_{l.*.1} \text{ else } e_{l.*.2}$) specifies that if the element e_l matches the pattern p_{tt} with the variables $v_{r.*}$ and the condition c_{nd} is true for the corresponding values of these variables, then the sequence $e_{l.*.1}$ is executed for these values of the variables. If e_l does not match p_{tt} , then the sequence $e_{l.*.2}$ is executed. The predefined CTSL element ($e_{l.1} = e_{l.2}$) specifies that $e_{l.1}$ and $e_{l.2}$ are equal.

The elements ($\text{return } e_l$) and (return) representing the queries return $[r_{p,q}^- e_l]$; and $\text{return};$ are defined by the rules

(rule ($\text{return } x$) $\text{var } (x) \text{ abn val } (x) \text{ then}$
 (let $w1$ be $(0 : \text{type}) :: \text{state} :: \text{function}$ in
 (if $(w1 :: q = \text{void} :: q) \text{ then und else}$
 (let $w2$ be $(\text{cast } x :: * :: q \ w1)$ in
 ($\text{type} : \text{return}, \text{value} : w2 :: q :: \text{ex}$)))));
 (rule (return) abn then
 (if $((0 : \text{type}) :: \text{state} :: \text{function} = \text{void} :: q)$
 then $(\text{type} : \text{return}) :: \text{ex else und}$)).

The predefined CTSL element ($\text{if } c_{nd} \text{ then } e_{l.*.1} \text{ else } e_{l.*.2}$) specifies that if the value of c_{nd} is true, then the sequence $e_{l.*.1}$ is executed. Otherwise, the sequence $e_{l.*.2}$ is executed. The predefined CTSL element ($\text{let } v_r \text{ be } e_l \text{ in } e_{l.*}$) is a shortcut for ($\text{let} :: \text{seq } (v_r) \text{ be } (e_l) \text{ in } e_{l.*}$).

The element ($\text{block } e_{l.*}$) representing the query $\{[r_{p,q}^- e_{l.*}]\}$ is defined by the rule

(rule ($\text{block } x$) $\text{var } (x) \text{ abn then}$
 $\text{enter-block}, (\text{let} :: \text{seq } (w1, w2)$
 be $((\text{block-variables in } (x)), (\text{block-labels in } (x))) \text{ in}$
 $x, (\text{continue-block in } w2, (x))$
 $(\text{catch} :: u \ w \ (\text{exit-block in } w1), (\text{throw } w))))$).

The element enter-block specifying the actions executed when the current configuration enters the block is defined by the rule

(rule $\text{enter-block abn then current-scope} + +$).

The element $\text{current-scope} + +$ is defined by the rule

(rule *current-scope ++ abn then*
 $((0 : scope) :: state :: block ::= ((0 : scope) :: state :: block + 1)))$).

The predefined CTSL element ($c_{nptl} ::= e_l$) assigns the value of e_l to the conceptual c_{nptl} . The predefined CTSL element ($e_{l.1} + e_{l.2}$) specifies the sum of $e_{l.1}$ and $e_{l.2}$.

The element (*block-variables in* ($e_{l.*}$)) returning the sequence of the local variables defined in declaration statements that are the elements of $e_{l.*}$ is defined by the rules

(rule (*block-variables in* ((*var* x y) z)) *var* (x , y) *seq* (z) *abn then*
where ((x is *variable-literal*) and (y is *type*)) *then*
 $(x :: q . + (block-variables in (z)))$);
(rule (*block-variables in* (x y)) *var* (x) *seq* (y) *abn then*
 $(block-variables in (y))$);
(rule (*block-variables in* ()) *abn then* ()).

The predefined CTSL element ($e_l . + (e_{l.*})$) adds the element e_l to the head of the sequence ($e_{l.*}$).

The element (*block-labels in* ($e_{l.*}$)) returning the sequence of the labels that are the elements of $e_{l.*}$ is defined by the rules

(rule (*block-labels in* ($x :: label$ y)) *var* (x) *seq* (y) *abn then*
 $(x :: label :: q . + (block-labels in (y)))$);
(rule (*block-labels in* (x y)) *var* (x) *seq* (y) *abn then*
 $(block-labels in (y))$);
(rule (*block-labels in* ()) *abn then* ()).

The element (*continue-block in* $l_{b.(*)}$, $e_{l.(*)}$) handling *goto* exceptions when the current configuration reaches the end of the block is defined by the rule

(rule (*continue-block in* x , (y)) *var* (x) *seq* (y) *und then*
catch w
if w *matches* (*type* : *goto*, *label* : z) :: *ex var* (z)
where ($z :: q$ *in* :: *set* x)
then (*throw* w), y , (*continue-block in* x , (y)) *else* (*throw* w))).

The element (*exit-block in* $v_{r.(*)}$) specifying the actions executed when the current configuration exits the block is defined by the rule

(rule (*exit-block in* x) *var* (x) *und then* (*catch* w
 $(delete-variables in x)$, *current-scope* --, (*throw* $w :: q$))).

The element *current-scope --* is defined by the rule

(rule *current-scope -- abn then*
 $((0 : scope) :: state :: block ::= ((0 : scope) :: state :: block - 1)))$).

The predefined CTSL element ($e_{l.1} - e_{l.2}$) specifies the difference between $e_{l.1}$ and $e_{l.2}$.

The element (*delete-variables in* ($v_{r.*}$)) deleting the local variables $v_{r.*}$ in $\llbracket \text{current-scope, current-call-level} \rrbracket$ is defined by the rule

```
(rule (delete-variables in x) var (x) abn then
  (let :: seq (w1, w2) be (current-scope, current-call-level) in
    (foreach y in x :: q do
      ((-3 : w2, -2 : w1, -1 : pointer, 0 : y, 1 : variable) ::=),
      ((-3 : w2, -2 : w1, 0 : y, 1 : variable) ::=))))).
```

The predefined CTSL element ($c_{ncptl} ::=$) is a shortcut for ($c_{ncptl} ::= \text{und}$). The predefined CTSL element (*foreach* v_r in ($e_{l.*}$) do b_d), where $b_d \in E_{l.*}$, executes sequentially the body b_d for each value of the variable v_r taken from the sequence $e_{l.*}$ from left to right.

The elements (e_l ";"") and ";" representing the queries $[r_{p,q}^- e_l]$; and ; are defined by the rules

```
(rule (x ";"") var (x) abn then x);
(rule ";" var (x) abn then)
```

The element (*if* :: C c_{nd} then $e_{l.1}$ else $e_{l.2}$) representing the query *if* $[r_{p,q}^- (c_{nd})]$ then $[r_{p,q}^- e_{l.1}]$ else $[r_{p,q}^- e_{l.2}]$ is defined by the rule

```
(rule (if :: C x then y else z) var (x, y, z) abn
  then (if ((cast x int) != 0) then (block y) else (block z))).
```

Other switch statements are defined in a similar way.

The element (*while* :: C c_{nd} do e_l) representing the query (*while* ($[r_{p,q}^- c_{nd}]$) $[r_{p,q}^- e_l]$) is defined by the rule

```
(rule (while :: C x do y) var (x, y) abn then
  (while ((cast x int) != 0)
    do (block y, (delete-exception continue))),
  (delete-exception break)).
```

The predefined CTSL element (*while* c_{nd} do b_d), where $b_d \in E_{l.*}$, executes the body b_d until the condition c_{nd} becomes the false value. Other iteration statements are defined in a similar way.

8.2. Declarations

The element (*function* f_n ($a_{rg.1} : t_{p.1}, \dots, a_{rg.n_t.0} : t_{p.n_t.0}$) : t_p b_d) representing the query $[r_{p,q}^- t_p]$ $[r_{p,q}^- f_n]$ ($[r_{p,q}^- t_{p.1}]$ $[r_{p,q}^- a_{rg.1}], \dots, [r_{p,q}^- t_{p.n_t.0}]$ $[r_{p,q}^- a_{rg.n_t.0}]$) $\{[r_{p,q}^- b_d]\}$ is defined by the rule

(rule (function x y : z u) var (x, y, z) seq (u) abn
where ((x is function-literal) and (y is attribute-element) and
(z is type))
then (let w be (values in y) in
(if ((w is (sequence type)) and
(not (-1 : w, 0 : x, 1 : function) :: function)) then
((-2 : arguments, -1 : w, 0 : x, 1 : function) :: function ::=
(attributes in y)),
((-2 : return-type, -1 : w, 0 : x, 1 : function) :: function ::=
z :: q),
((-2 : body, -1 : w, 0 : x, 1 : function) :: function ::= (u :: q),
((-1 : w, 0 : x, 1 : function) :: function ::= true)))
else und)).

The predefined CTSL element (*e_l is attribute-element*) specifies that *e_l* is an attribute element. The predefined CTSL elements (*attributes in e_{l.a}*) and (*values in e_{l.a}*) specify the sequence of attributes in the attribute element *e_{l.a}* and the sequence of their values, respectively. The predefined CTSL element (*not c_{nd}*) specifies the negation of *c_{nd}*.

The element (*var v_r t_p*) representing the query $[r_{p,q}^- t_p] [r_{p,q}^- v_r]$; is defined by the rule

(rule (var x y) var (x, y) abn
where ((x is variable-literal) and (y is type))
then (let :: seq (w1, w2) be (current-scope, current-call-level) in
(if (-2 : w1, -1 : w2, 0 : x, 1 : variable) then und else
((-3 : type, -2 : w1, -1 : w2, 0 : x, 1 : variable) ::= y :: q),
((-2 : w1, -1 : w2, 0 : x, 1 : variable) ::= true))).

The element (*struct t_{p.s} (f_{l.1} : t_{p.1}, ..., f_{l.n_t} : t_{p.n_t})*) representing the query *struct* $[r_{p,q}^- t_{p.s}] \{ [r_{p,q}^- t_{p.1}] [r_{p,q}^- f_{l.1}]; \dots; [r_{p,q}^- t_{p.n_t}] [r_{p,q}^- f_{l.n_t}] \}$ is defined by the rule

(rule (struct x y) var (x, y) abn where
((x is structure-type-literal) and (y is attribute) and
(let w be (attributes in y) in (w is (sequence field-literal)))
and (let w be (attribute-values in y) in (w is (sequence type))))
then (if (x is structure-type) then und
else ((-1 : body, 0 : x, 1 : structure-type) ::= y :: q),
((0 : x, 1 : structure-type) ::= true))).

8.3. Expressions

The element *v_l* representing the query *v_l* is defined by the rule

(rule x var (x) abn where (x is value-literal) then (throw x :: q)).

The element v_r representing the query $[r_{p,q}^- v_r]$ is defined by the rule

(rule x var (x) abn then (let :: seq $(w1, w2)$ be
 ((index in x), (current-call-level in $w1$)) in
 (-3 : value, -2 : $w2$, -1 : $w1$, 0 : x , 1 : variable))).

The element (current-call-level in s_{cp}) is defined by the rule

(rule (current-call-level in x) var (x) abn where (x is scope) then
 (if $(x :: q = 0)$ then 0 else current-call-level)).

The element $(e_l [e_{l.1}])$ representing the query $[r_{p,q}^- e_l][[r_{p,q}^- e_{l.1}]]$ is defined by the rule

(rule $(x [y])$ var (x, y) abn val (y, x) where ($x :: *$ is array)
 then (let w be (cast $y :: * int$) in (if $(w$ and $(w :: q >= 0)$)
 then $((-1$: body, 0 : $x :: *$, 1 : array) . $(w + 1))$ else und))).

The predefined CTSL element $(e_{l.1} >= e_{l.2})$ specifies that $e_{l.1}$ is greater than or equal to $e_{l.2}$. The predefined CTSL element $((e_{l.*}) . n_t)$ specifies the n_t -th element of the sequence $e_{l.*}$.

The element $(e_l . :: C f_l)$ representing the query $[r_{p,q}^- e_l].[r_{p,q}^- f_l]$ is defined by the rule

(rule $(x . :: C y)$ var (x, y) abn val (x) where
 ($x :: *$ is structure) and (y is field-literal)) then
 $((-1$: body, 0 : $x :: *$, 1 : structure) .. y)).

The element $(e_l := e_{l.1})$ representing the query $[r_{p,q}^- e_l] := [r_{p,q}^- e_{l.1}]$ is defined by the rule

(rule $(x := y)$ var (x, y) abn val (y) then
 (let :: seq $(w1, w2, w3, w4)$ be ((left-hand in x),
 ($w1$.. left), ($w1$.. type), (cast $y :: * :: q w3$)) in
 (if $(w1$ and $w4)$ then $(w2 := w4 :: q)$ else und))).

The element (left-hand in e_l) is defined by the rule

(rule (left-hand in x) var (x) abn then (let $w1$ be (index in x) in
 (if $w1$ then (let :: seq $(w2, w3)$ be ((current-call-level in $w1$),
 (-3 : type, -2 : $w2$, -1 : $w1$, 0 : x , 1 : variable)) in
 (left : (-3 : value, -2 : $w2$, -1 : $w1$, 0 : x , 1 : variable),
 type : $w3$) :: q)
 elseif x matches $(* y)$ var (y) val (y) then
 (if $(y :: *$ is typed-pointer) then (let $w2$ be $(y :: * :: q$.. type) in
 (left : (-1 : value, 0 : $y :: *$, 1 : pointer), type : $w2$) :: q))
 elseif $(y :: *$ is variable-pointer) then
 (let :: seq $(w2, w3, w4, w5)$

```

    be ((y :: * .. variable), (y :: * .. scope), (y :: * .. call-level),
        (-3 : type, -2 : w4, -1 : w3, 0 : w2, 1 : variable)) in
    (left : (-3 : value, -2 : w4, -1 : w3, 0 : w2, 1 : variable),
        type : w5) :: q)
elseif (y :: * is array-pointer) then (let :: seq (w2, w3, w4)
    be ((y :: * .. array), (y :: * .. index),
        (-1 : element-type, 0 : w2, 1 : array)) in
    (left : ((-1 : body, 0 : w2, 1 : array) . w3 :: q), type : w4) :: q)
elseif (y :: * is structure-pointer) then
    (let :: seq (w2, w3, w4, w5)
        be ((y :: * .. structure), (y :: * .. field),
            (-1 : type, 0 : w2, 1 : structure),
            ((-1 : body, 0 : w4, 1 : structure-type) .. w3)) in
        (left : ((-1 : body, 0 : w2, 1 : structure) .. w3), type : w5) :: q)
    else und)
elseif x matches (y .: C z) var (y, z) val (y)
    where (y :: * is structure) then (let :: seq (w2, w3) be
        ((-1 : type, 0 : y :: *, 1 : structure),
            ((-1 : body, 0 : w2, 1 : structure-type) .. z)) in
        (if w3 then
            (left : ((-1 : body, 0 : y :: *, 1 : structure) .. z), type : w3) :: q
            else und))
elseif x matches (y [ z ]) var (y, z) val (z, y)
    where (y :: * is array) then (let :: seq (w2, w3, w4) be
        ((-1 : element-type, 0 : y :: *, 1 : array), (cast z :: * int),
            (-1 : length, 0 : y :: *, 1 : array)) in
        (if ((w2 is type) and w3 and (w3 :: q >= 0) and
            (w3 :: q < w4 :: q)) then
            (left : ((-1 : body, 0 : y :: *, 1 : array) . z :: * :: q),
                type : w4) :: q else und))
    else und))).
    
```

The predefined CTSL element $(e_{l,1} < e_{l,2})$ specifies that $e_{l,1}$ is less than $e_{l,2}$. The predefined CTSL element $(if\ c_{nd}\ then\ e_{l,*}\ elseif\ c_{nd,1}\ e_{l,*,1})$ is a shortcut for $(if\ c_{nd}\ then\ e_{l,*}\ else\ (if\ c_{nd,1}\ e_{l,*,1}))$.

Let $e_{l,*} \# c_{nf}$ be a shortcut for $[c_{nf}\ (0 : ()) :: state :: program : (e_{l,*})]$. Let $e_{l,*} \# v_l \# c_{nf}$ be a shortcut for $[c_{nf}\ (0 : ()) :: state :: program : (e_{l,*}), (0 : ()) :: state :: value : v_l]$. The atoms *program* and *value* are the names of the substates of configurations in CTSL specifying the information about programs and the returned values in CTSL [7]. The conceptals $(0 : ()) :: state :: program$ and $(0 : ()) :: state :: value$ store the current program and the returned value, respectively.

The element $(cast\ e_l\ t_p)$ representing the query $([r_{p,q}^- t_p]) [r_{p,q}^- e_l]$ is defined as follows:

(rule $(cast\ x\ y)\ var\ (x,\ y)\ abn\ val\ (x)\ where\ (y\ is\ type)$
 then $(cast\ x\ ::\ * \ y) :: atm$);
 (transition $(cast\ x\ y) :: atm\ var\ (x,\ y)\ then\ f_n$),

where

- if $[r_{p,a}^- v_l]$ is a result of conversion of $[r_{p,q}^- x_0]$ to $[r_{p,q}^- y_0]$, then $(cast\ x_0\ y_0) :: atm$, $e_{l,*} \# c_{nf} \rightarrow_{f_n,(x:x_0,y:y_0)} e_{l,*} \# v_l \# c_{nf}$.

The syntax and semantics of atomic transitions is defined in [7].

The element $(e_l + :: C\ e_{l,1})$ representing the query $[r_{p,q}^- e_l] + [r_{p,q}^- e_{l,1}]$ which specifies the sum of numbers $[r_{p,q}^- e_l]$ and $[r_{p,q}^- e_{l,1}]$ of the type *int* is defined as follows:

(rule $(x + :: C\ y)\ var\ (x,\ y)\ abn\ val\ (x)$
 where $(x\ is\ int)$ and $(y\ is\ int)$ then $(x + :: C\ y) :: (int + int) :: atm$);
 (transition $(x + :: C\ y) :: (int + int) :: atm\ var\ (x,\ y)\ then\ f_n$),

where

- if $[r_{p,a}^- v_l]$ is the result of addition of $[r_{p,q}^- x_0]$ and $[r_{p,q}^- y_0]$ returned by AM[C], then $(x_0 + :: C\ y_0) :: (int + int) :: atm$, $e_{l,*} \# c_{nf} \rightarrow_{f_n,(x:x_0,y:y_0)} e_{l,*} \# v_l \# c_{nf}$.

The elements $(new\ t_p)$ and $(delete\ p_{n,t})$ representing the dynamic memory management queries are defined by the rules

(rule $(new\ x)\ var\ (x)\ abn\ where\ (x\ is\ type)$ then
 (let w be $(new\ pointer-id)$ in
 $((0 : (id : w,\ type : x) :: pointer,\ 1 : pointer) ::= true)$,
 $(id : w,\ type : x) :: q$);
 (rule $(delete\ x)\ var\ (x)\ abn\ val\ (x)$
 where $(x :: * is\ typed-pointer-literal)$ then
 $((-1 : value,\ 0 : x :: *,\ 1 : pointer) ::=)$,
 $((0 : x :: *,\ 1 : pointer) ::=)$).

The element $(new-cc\ c_{ncp,c})$ generates a new instance of the countable concept $c_{ncp,c}$ [7]. The element $pointer-id$ is a countable concept specifying unique identifiers of addresses.

We have considered the ways of constructing the definitions for C expressions by the examples of some C operators. The construction of a definition for a function call can be found in [3]. The definitions for other C operators are constructed in a similar way.

8.4. Programs

The element sequence $e_{l.1} \dots e_{l.n_t}$ represents the program $[r_{p,q}^- e_{l.1}] \dots [r_{p,q}^- e_{l.n_t}]$ in C.

9. Conclusion

The method presented in this paper describes the stepwise well-defined process of operational semantics development for imperative programming languages. Therefore, it can become a basis of the technology of operational semantics development for this class of languages.

The fragment of the C language used as the case study for this method covers a representative set of constructs of procedural programming languages. Thus, the paper can be also considered as a cookbook on the development of operational semantics for procedural programming languages.

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